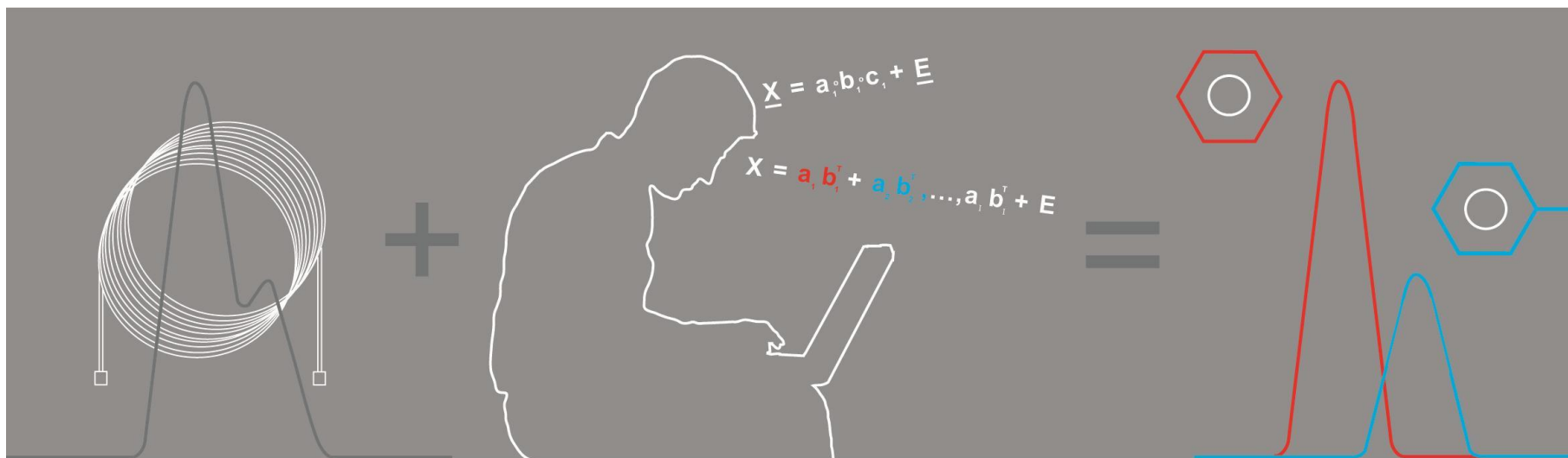




# Practical Problems in Tensor Modeling

(In chemometrics)

Rasmus Bro





Dioxin,  
Environment,  
Dose-response

Food quality,  
Raw material influence,  
Production optimization



Genomics,  
Systems biology,  
Cancer,  
Diabetes,  
Pharma

...

# What we work with



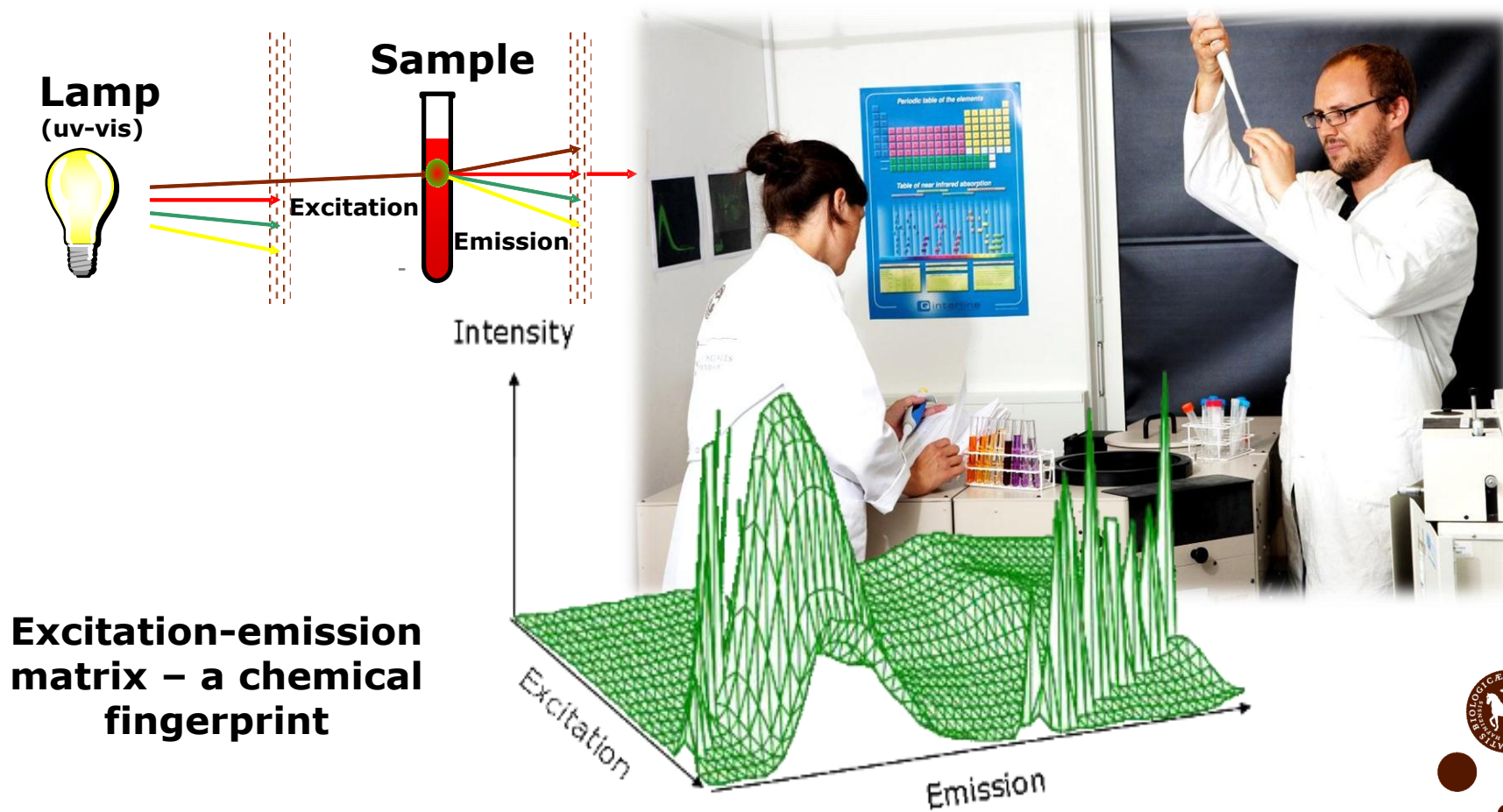


**Fluorescence**  
**High resolution NMR**  
**Mass spectrometry**  
**Near-infrared**  
**Raman**  
**Ultrasound**  
**Hyperspectral Imaging**  
**Chromatography**  
**Imaging**

...

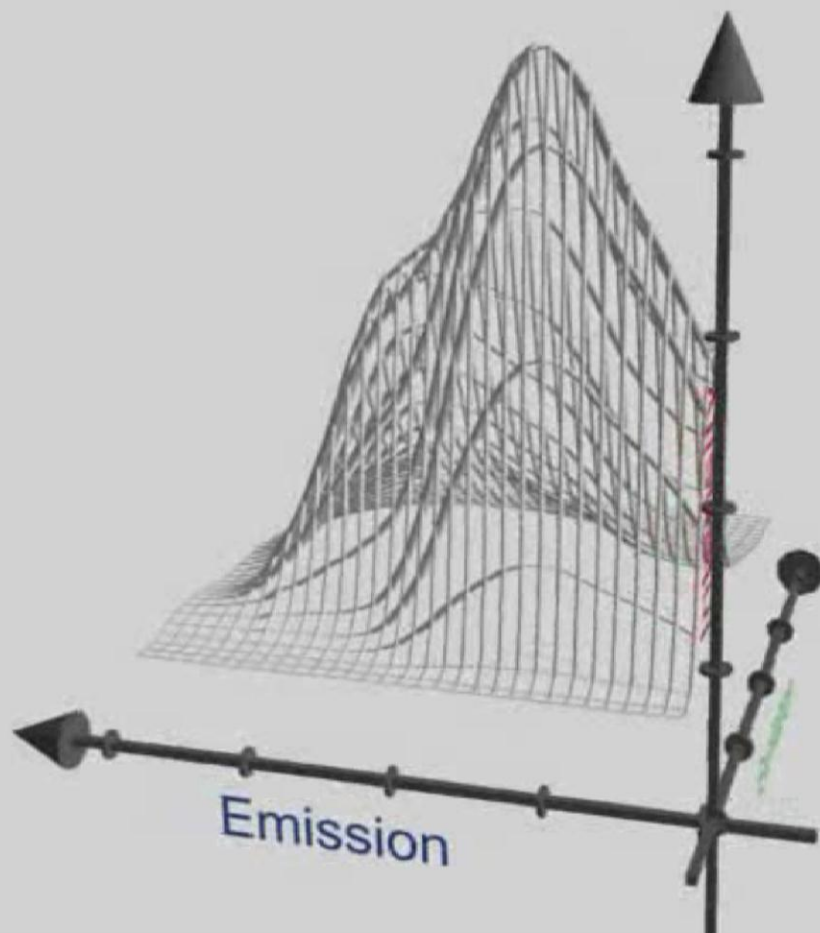
**Data**

# Fluorescence



# Fluorescence

Food Technology - LMT - KVL - <http://models.kvl.dk>



Excitation  
matrix

fingerprint

Excitation

Emission



# Basic Plotting Uncertainty estimates Automated analysis problems



# Interpretation

How to interpret  
a scatter plot



[www.models.kvl.dk](http://www.models.kvl.dk)

	Workload	Distance to work	Salary
Smith	1.0	0.2	1.2
Johnson	2.0	0.0	0.3
Williams	-1.0	0.1	-1.0
Jones	-2.0	0.2	-0.1
Davis	0.0	-0.4	-0.4



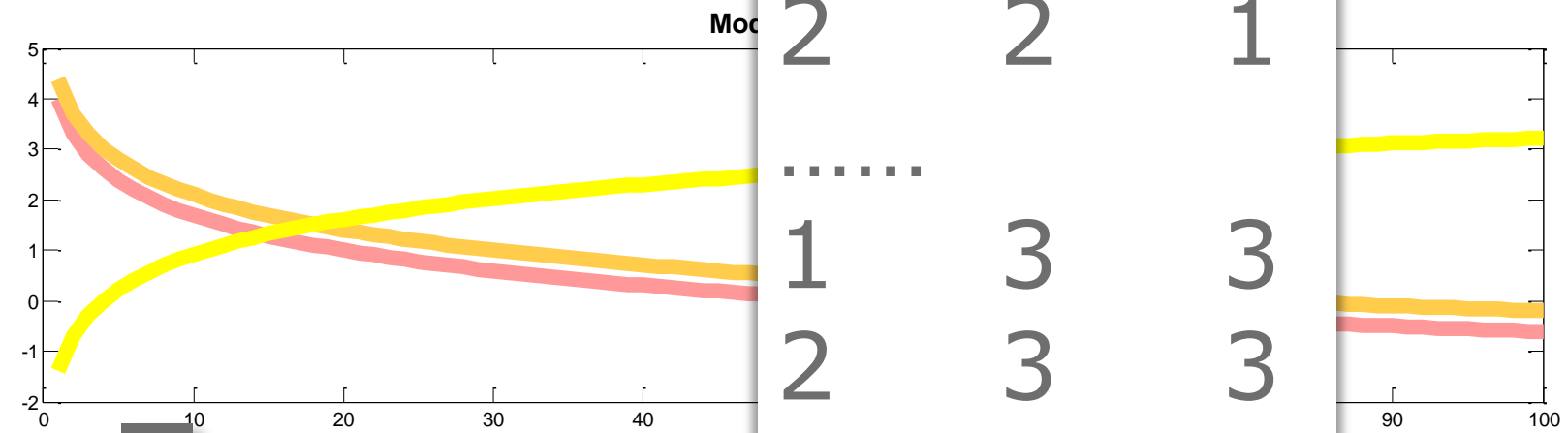
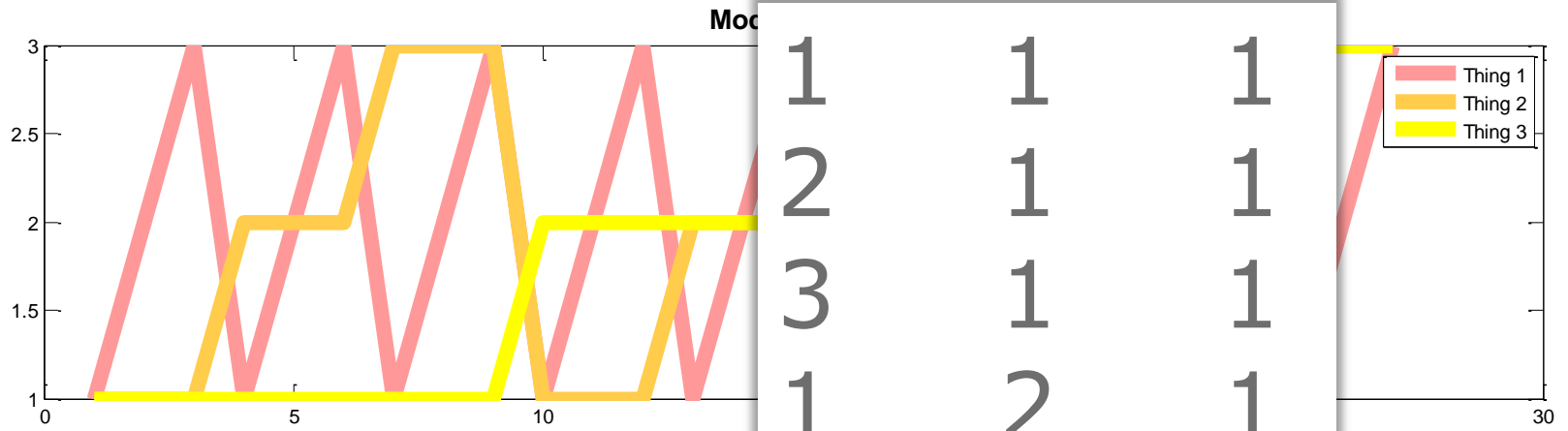
# Plotting

- Two-way PCA - orthonormal basis (loadings)
- Hence distances in scores reflect both manifest and latent distances
  
- PARAFAC/Tucker - Oblique bases
- Distances reflect only latent distances not manifest

# Plotting



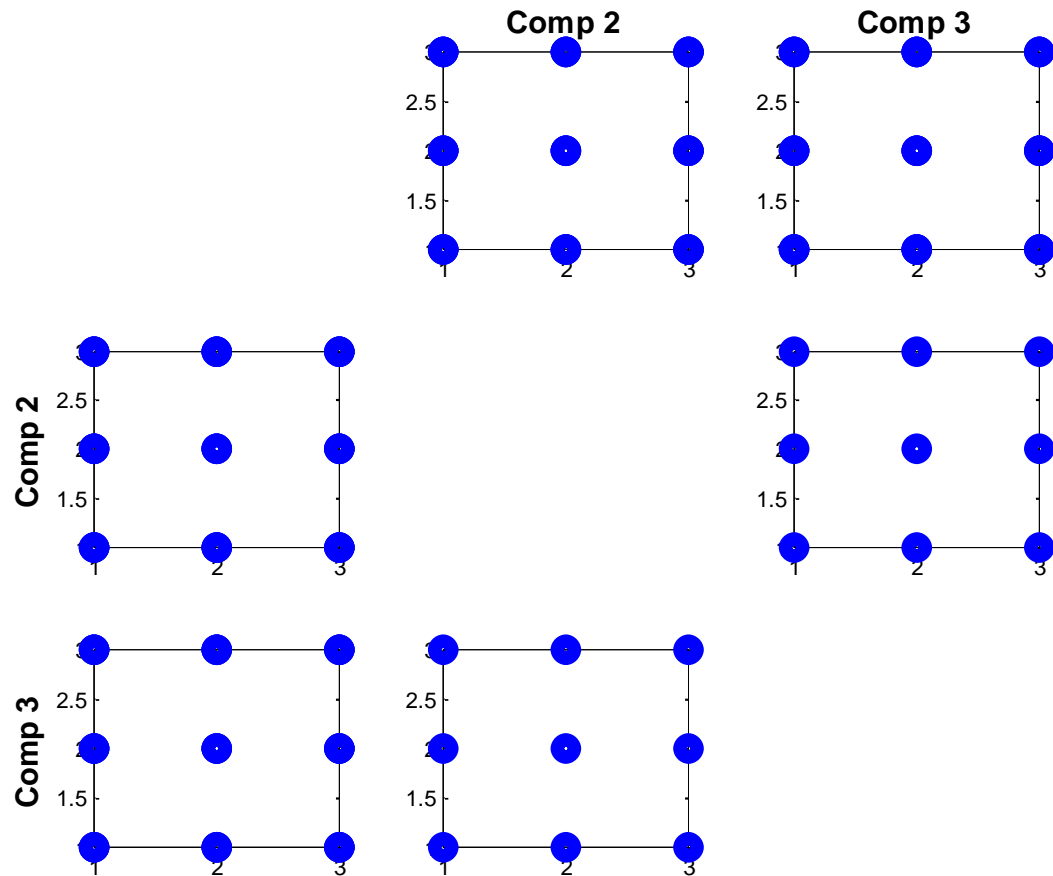




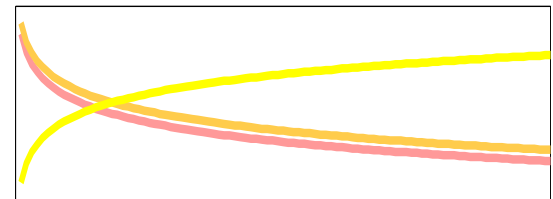
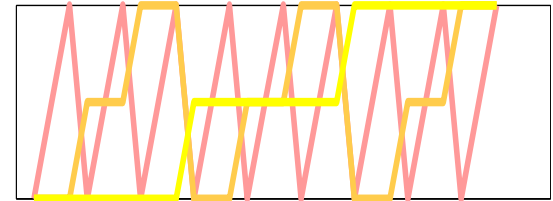
1	1	1
2	1	1
3	1	1
1	2	1
2	2	1
.....		
1	3	3
2	3	3
3	3	3

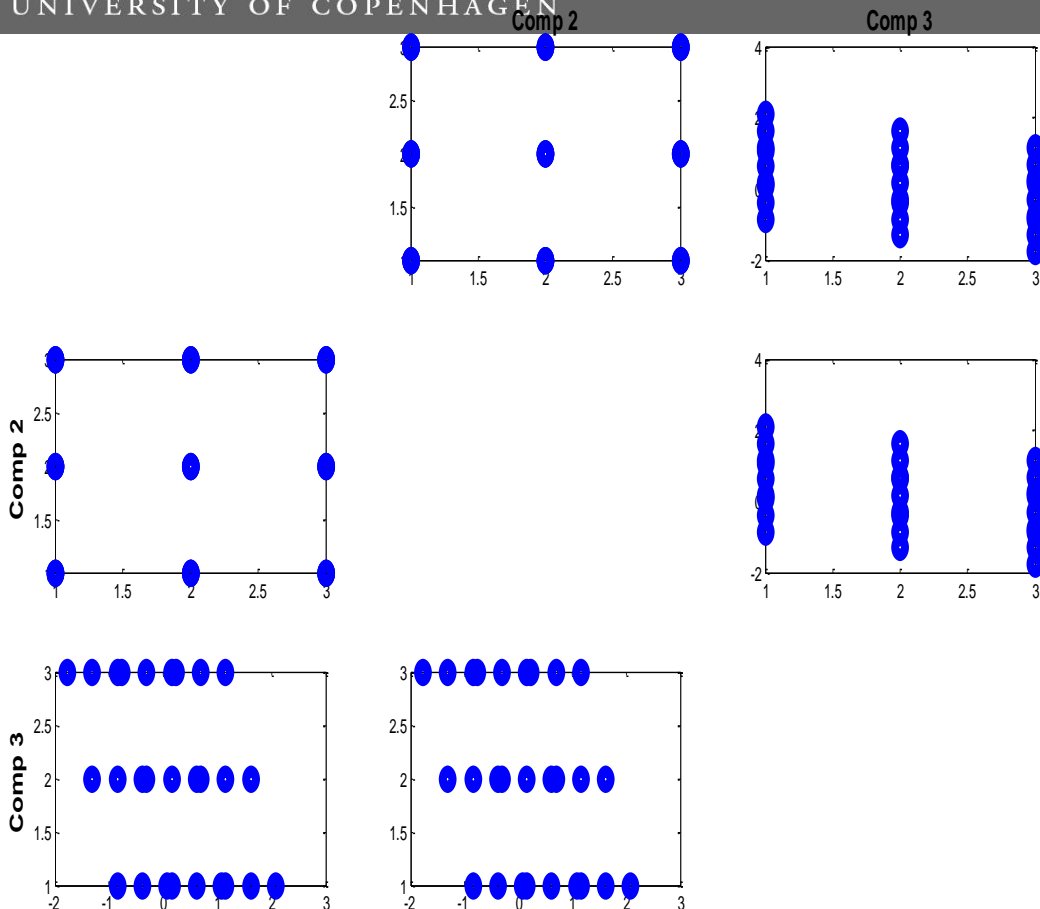
# Plotting



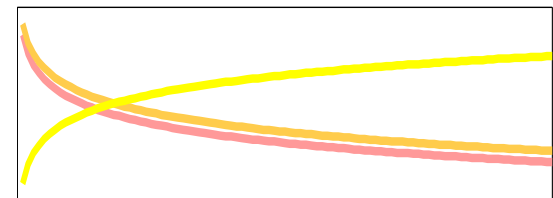
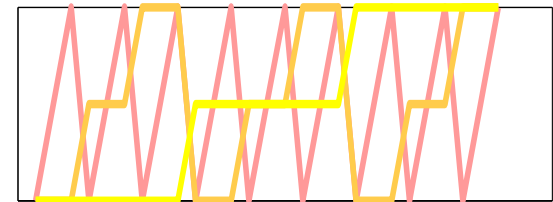
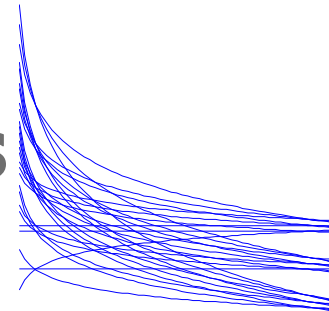


Plotting the first mode component in scatter plots reflecting *latent variation*





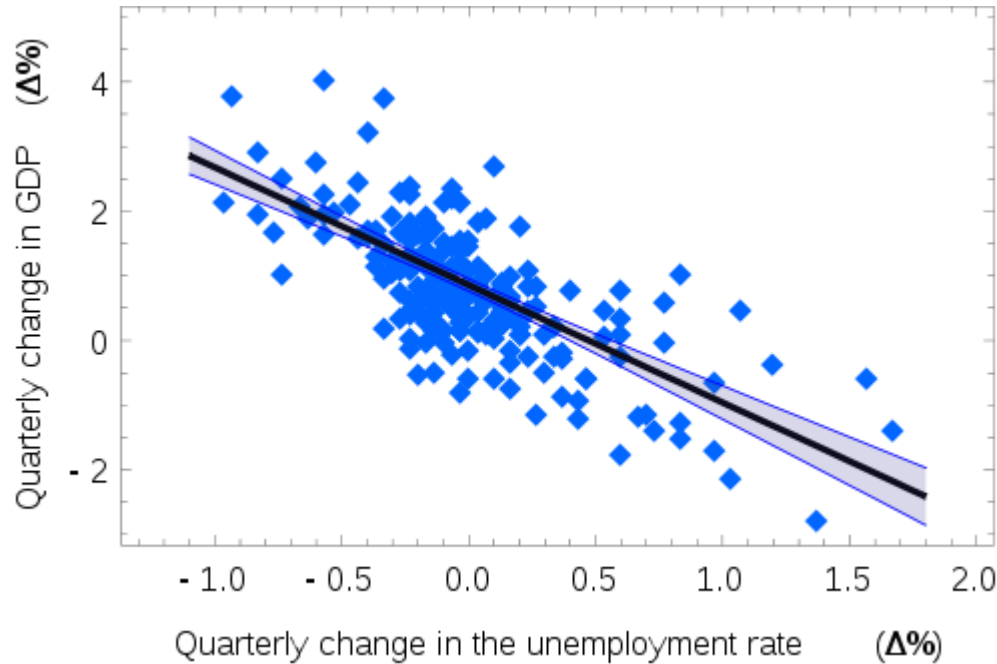
Plotting on an  
**orthogonal**  
**basis reflecting**  
**raw data**  
**distances**



# Uncertainty of parameters

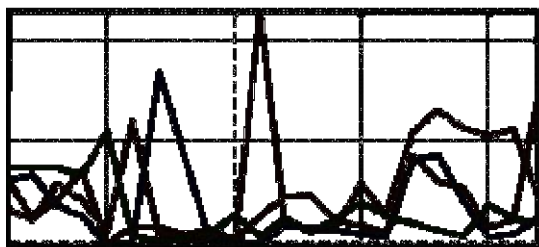
$$s^2 = \frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N-1}$$

No degrees of freedom in PARAFAC (and probably not in other multilinear models)

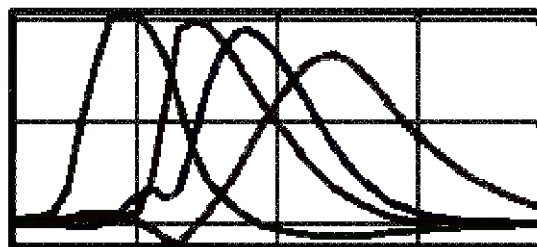


# PARAFAC on fluorescence

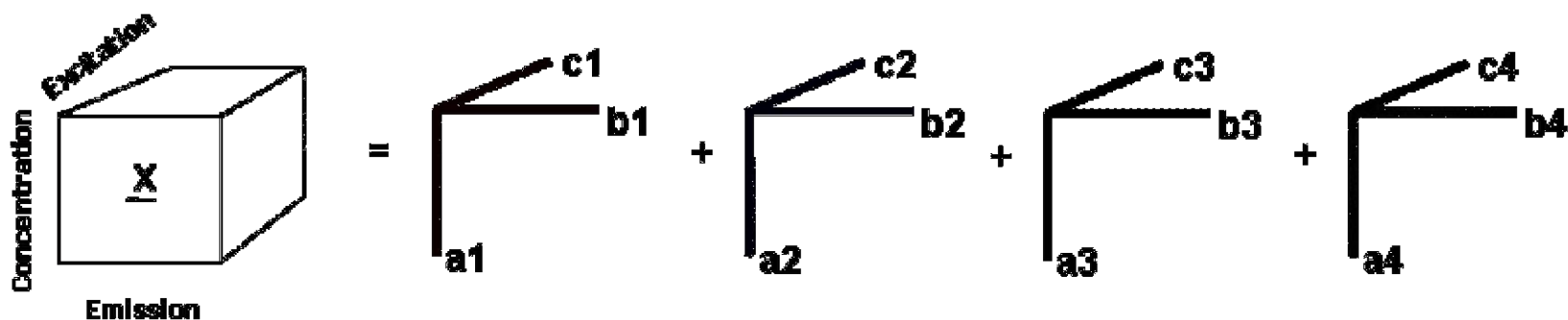
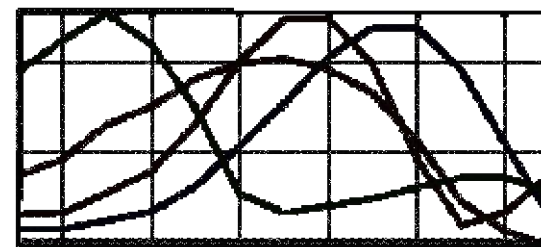
**A: Concentration**



**B: Emission**

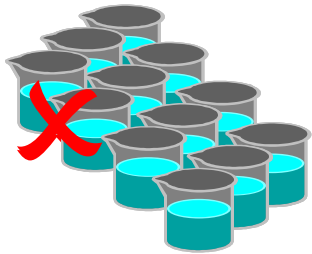


**C: Excitation**



# Jack-knifing the model

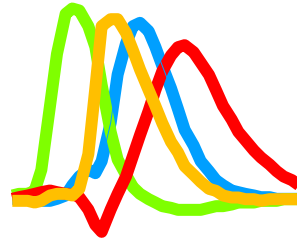
Leave out sample 1



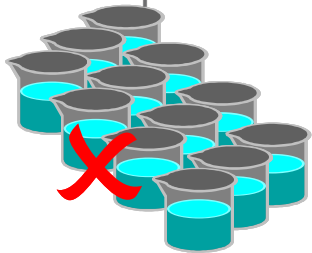
PARAFAC



1st jack-knife segment



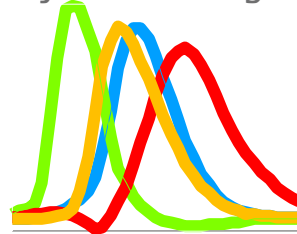
Sample 2



PARAFAC



2nd jack-knife segment



⋮

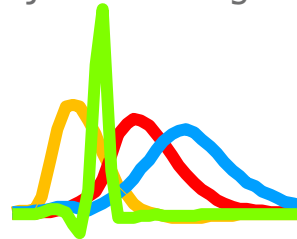
Sample I



PARAFAC



$l$ th jack-knife segment



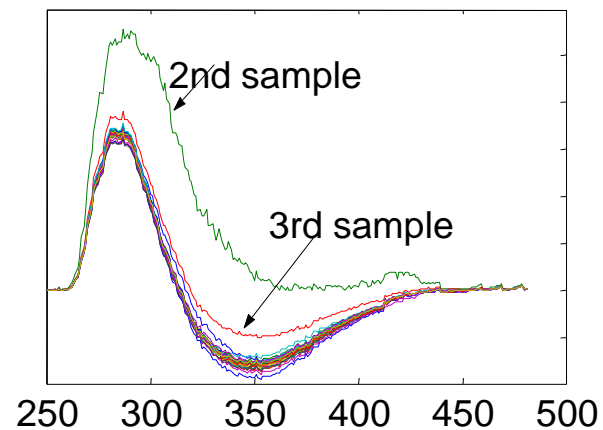
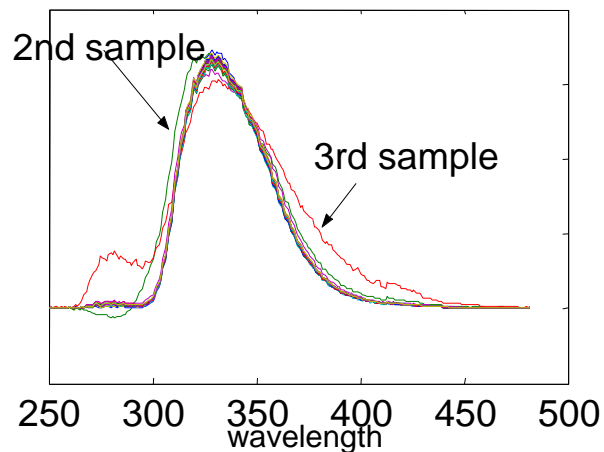
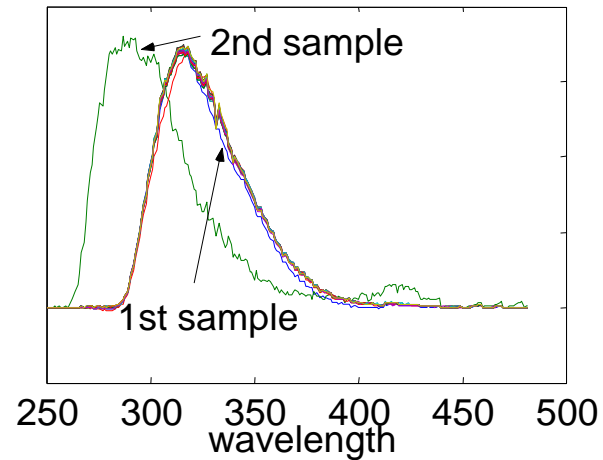
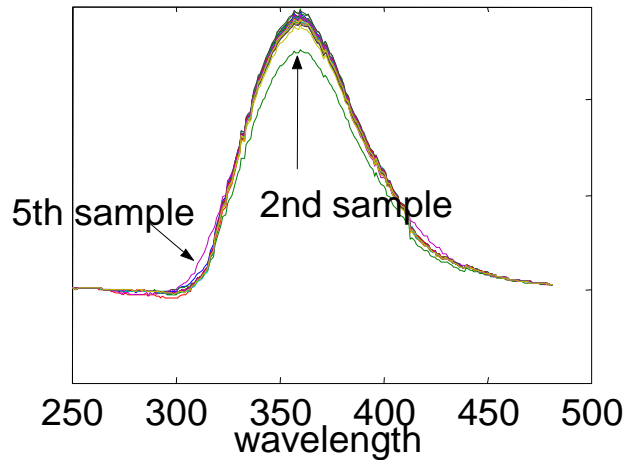
I PARAFAC sub-models:

- Standard error
- Outlier detection

J. Riu and R. Bro. Jack-knife technique for outlier detection and estimation of standard errors in PARAFAC models. *Chemom. Intell. Lab. Syst.* 65 (1):35-49, 2003.



# Jack-knifing the model

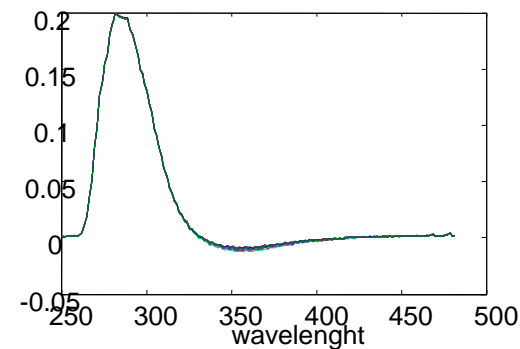
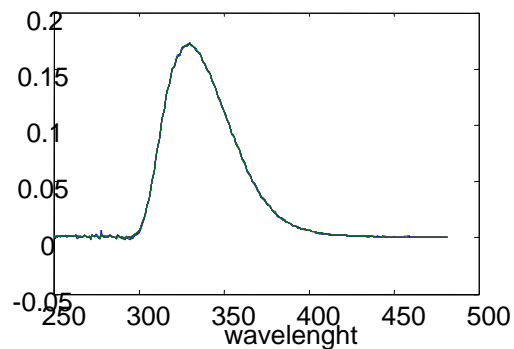
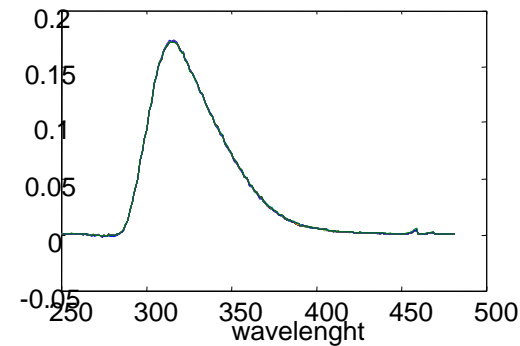
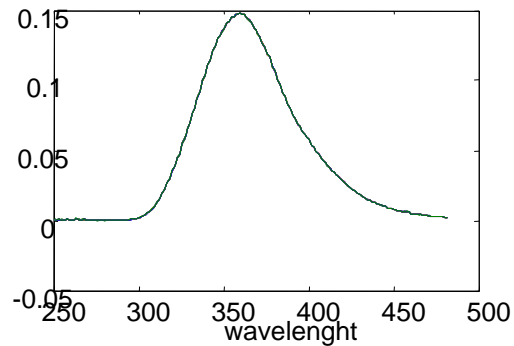


Emission spectral profiles



# Jack-knifing the model

Removing low excitation and  
sample #2,3,5,10



Emission spectral profiles





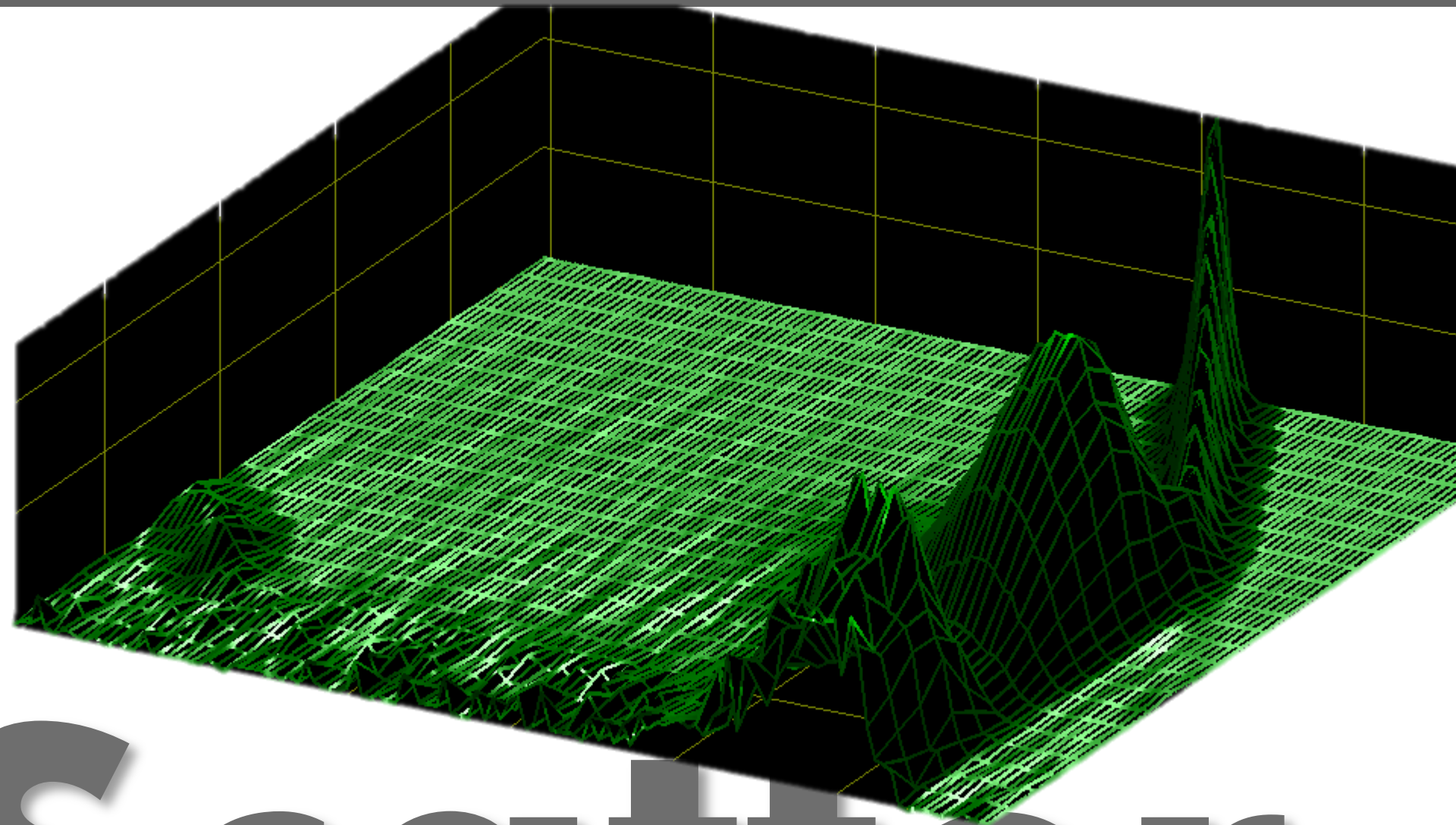
# Automatic ?

Meta-parameters

Goodness

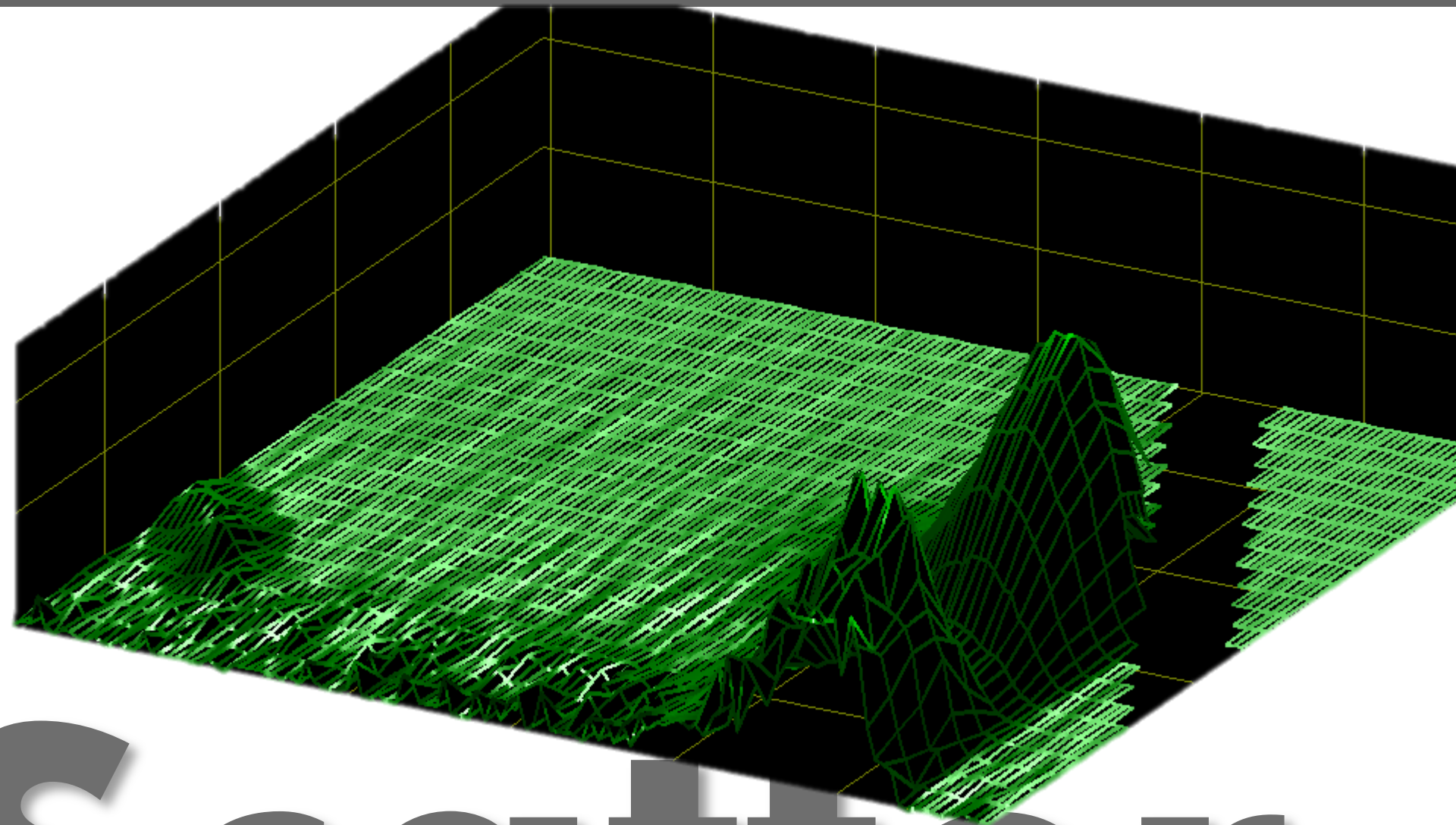
Result





# Scatterer





# Scatter



Long story ...

# Outliers



## Must be approximately valid

- Sufficient number of adequate samples
- Sufficient spectral resolution
- Beers law valid

## Then decide

- Low excitation wavelengths to exclude
- How to handle Rayleigh scattering
- Number of components to use
- Outliers to exclude

# EEMizer



## Goodness criterion

Goodness = Fit\*CoreConsistency\*Splithalf

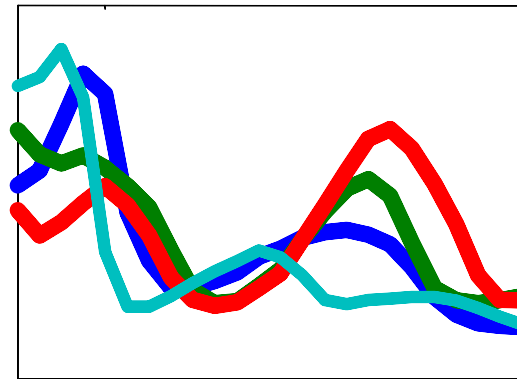
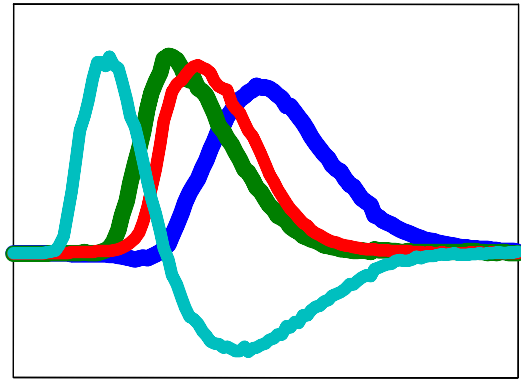
$$FIT = 1 - \frac{\sum_{i=1}^I \sum_{j=1}^J \sum_{k=1}^K e_{ijk}^2}{\sum_{i=1}^I \sum_{j=1}^J \sum_{k=1}^K x_{ijk}^2}$$

$$COREC = 100 \left( 1 - \frac{\sum_{d=1}^F \sum_{e=1}^F \sum_{f=1}^F (g_{def} - t_{def})^2}{F} \right)$$

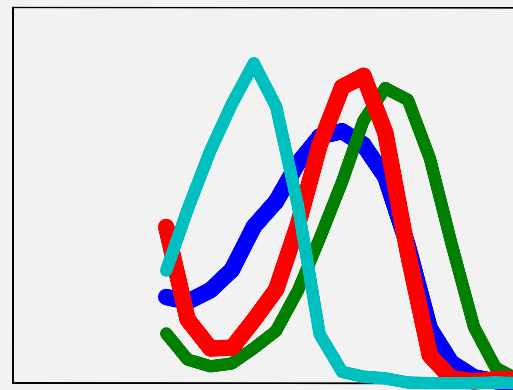
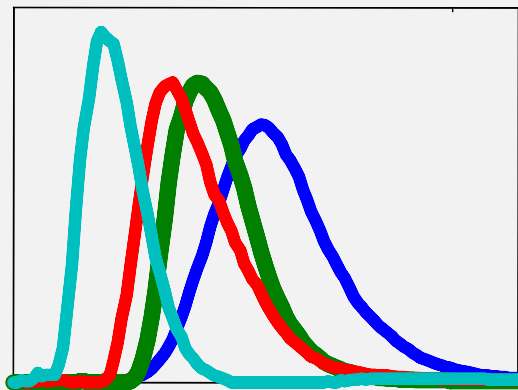
# EEMizer



## Before EEMizer



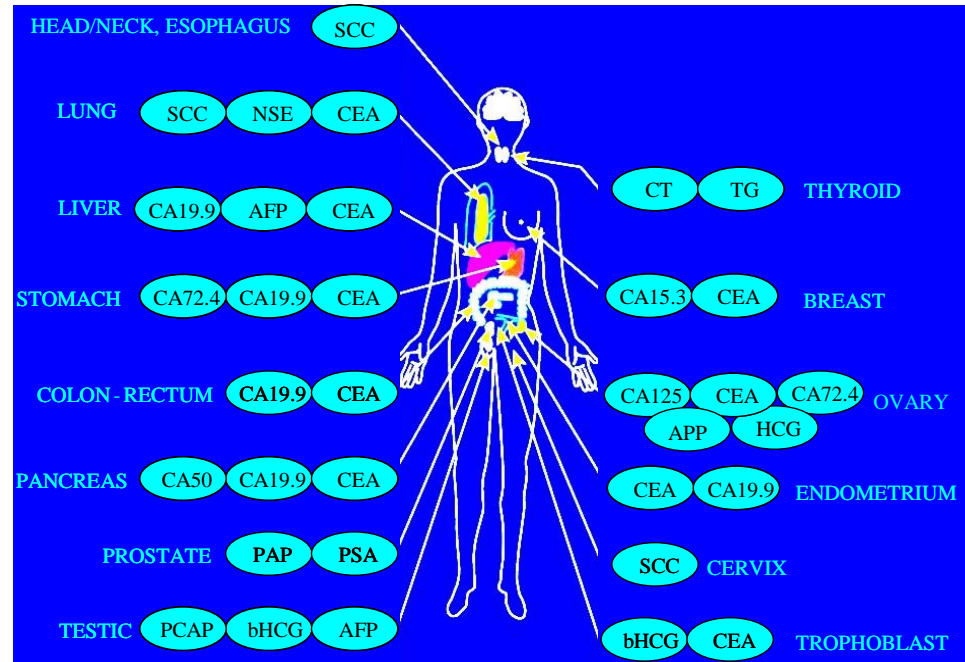
## After EEMizer



# EEMizer result.



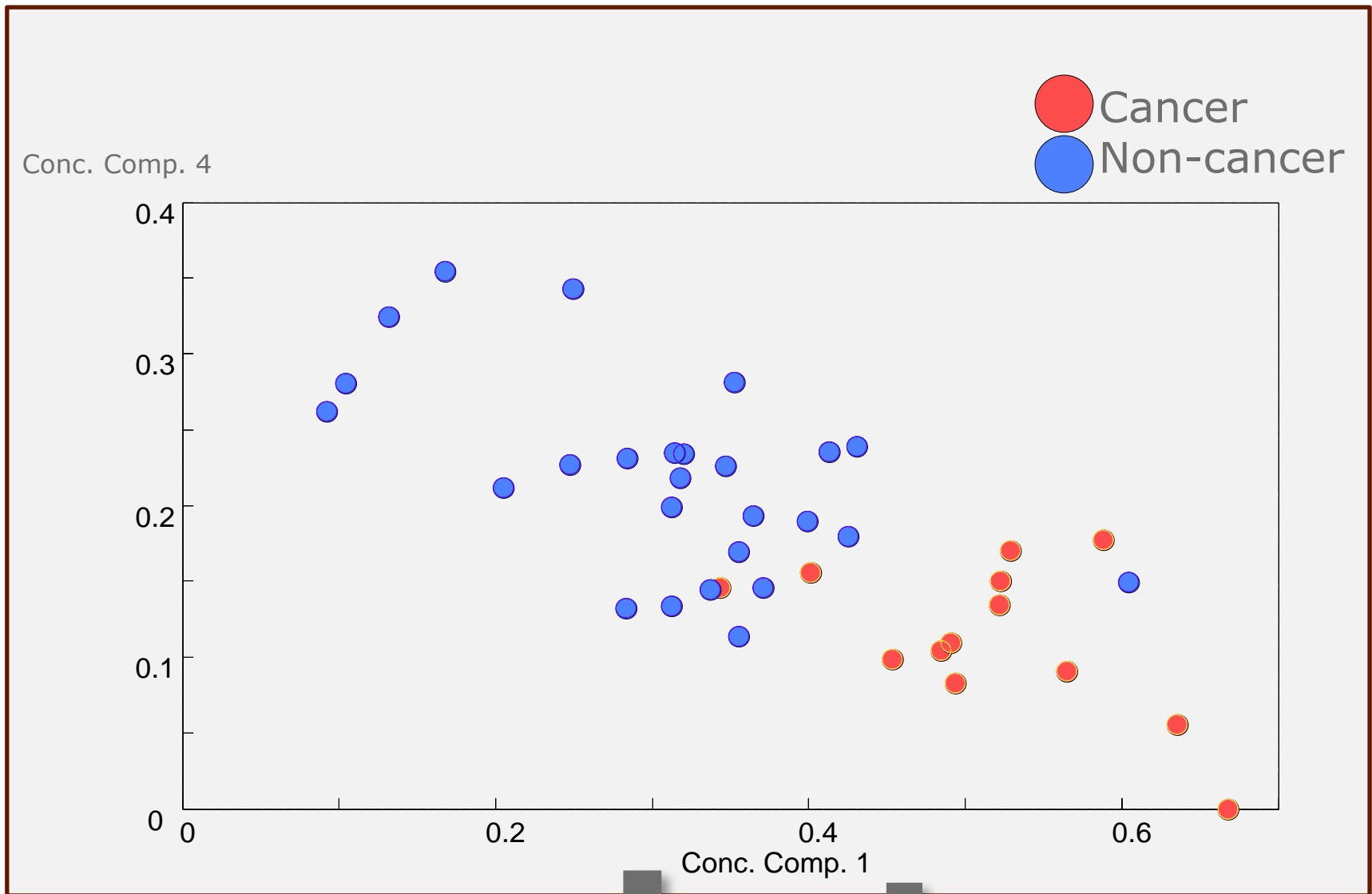
# Traditional approach for cancer diagnostics and monitoring: Biomarkers



# cancer







# It works!



# Conclusion

**Still needed**

Better algorithms

Better statistics

Better software



m-files, e-courses, data sets, etc.

**[www.models.life.ku.dk](http://www.models.life.ku.dk)**

If you want lots of papers on applied  
tensor analysis, come by with a USB

