

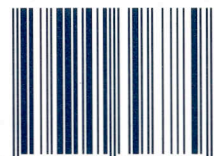
# Artificial Neural Networks for Modelling and Control of Non-Linear Systems

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Artificial neural networks possess several properties that make them particularly attractive for applications to modelling and control of complex non-linear systems. Among these properties are the universal approximation ability, the parallel network structure and the availability of on- and off-line learning methods for the interconnection weights. However, dynamical models that contain neural network architectures might be highly non-linear and as a result difficult to analyse. *Artificial Neural Networks for Modelling and Control of Non-Linear Systems* investigates the subject from a system theoretical point of view. However the mathematical theory that is required from the reader is limited to matrix calculus, basic analysis, differential equations and basic linear system theory. No preliminary knowledge of neural networks is explicitly required. Both classical and novel network architectures and learning algorithms for modelling and control are presented. Topics include non-linear system identification, neural optimal control, top-down model based neural control design and stability analysis of neural control systems. A major contribution of this book is to introduce *NLq Theory* as an extension towards modern control theory, in order to analyse and synthesize non-linear systems that contain linear together with static non-linear operators that satisfy a sector condition. Neural state space control systems are an example of this. Moreover, it turns out that *NLq Theory* is unifying with respect to any problems arising in neural networks, systems and control. Examples show that complex non-linear systems can be modelled and controlled within *NLq Theory*, including mastering chaos. The didactic flavour of this book makes it suitable for use as a text for a course on Neural Networks. In addition, researchers and designers will find many important new techniques, in particular *NLq Theory*, that have applications in control theory, system theory, circuit theory and Time Series Analysis.

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