

# INTEGRATIVE ANALYSIS OF DATA, LITERATURE, AND EXPERT KNOWLEDGE BY BAYESIAN NETWORKS

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- 1. The ovarian cancer problem, the IOTA project
- 2. Contributions

BUBS:Sy

- 3. Priors for the ovarian cancer problem
- 4. Text-mining by Bayesian networks
- 5. Bayesian analysis of relevance using Bayesian networks
- 6. Informative priors for black-box conditional models
- 7. Applications
- 8. Challenges
- 9. Publications, CV



- 1. The first/second most commonly diagnosed gynecologic malignancy.
- 2. The leading cause of death from gynecological malignancy.
- 3. The fifth leading cause of cancer deaths in women.
- 4. Poor prognosis if diagnosed at an advanced stage.
- 5.  $\Rightarrow$  Early diagnosis is important (screening, prevention).



(b) Understanding: Relevant variables/risk factors



#### The ovarian cancer problem

#### in the high-throughput context





# International Ovarian Tumor Analysis

# Consortium (IOTA)

- 1. Data (9-19 international centers)
  - (a) 68 parameters
  - (b) 1,066 cases IOTA 1(2007)
- 2. Models
  - (a) logistic regression (LR) (1997),
  - (b) multilayer perceptrons (MLPs) (1998),
  - (c) support vector machines (SVMs) (1998),
  - (d)  $\Rightarrow$ Bayesian logistic regression/multilayer perceptrons (2001),
  - (e)  $\Rightarrow$  Bayesian Belief networks (BNs) (2001),
  - (f) least squares support vector machines (2002),
  - (g) Bayesian kernel methods (2007)



- Parameters: 35 out of 68 are used in the thesis: FamHistBrCa, FamHistOvCa, FamHist, PMenoAge, ReprYears, Meno, Age, PostMenoY, Hysterectomy, CycleDay, PillUse, Parity, HormTherapy, Pathology, PapFlow, PapSmooth, Papillation, Solid, WallRegularity, Septum, IncomplSeptum, Locularity, Echogenicity, Shadows, TAMX, PSV, PI, RI, ColScore, Volume, Ascites, Fluid, Bilateral, Pain, CA125
- 2. Data sets in the thesis  $\neq IOTA 1$ (2007)
  - (a) *IDO*, 11 variables, 300 cases (1997)
    (b) *IOTA* 1.1, 31 variables, 604 cases (2002)
  - (c) IOTA 1.2, 35 variables, 782 cases (2003)

The biplot of the IOTA-1.2 data set: (variables:'**o**', cases:'+'/'o')

GDBS:SPUB



**Component 2** 



#### Models:

## Probabilistic conditional and domain models

Logistic regression (LR):  $P(y|\underline{x}) = \sigma[\sum_{i=0}^{n} (\beta_{i}x_{i} + \sum_{j=1}^{n} (\beta_{i,j}x_{i}x_{j} + \ldots)))],$ Multilayer perceptron (MLPs):  $f(\underline{x}, \underline{\omega}) = \sigma[\sum_{i=1}^{L} (\omega_{i} \tanh[\sum_{j=1}^{|\underline{X}|} (\omega_{ij}x_{j} + \omega_{i0})])],$ Naive Bayesian networks (N-BNs):  $p(y, x_{1}, \ldots, x_{n}|\underline{\theta}) = p(y) \prod_{i=1}^{n} p(x_{i}|y),$ Bayesian networks (BNs):  $p(x_{1}, \ldots, x_{n}|\underline{\theta}, G) = \prod_{i=1}^{n} p(x_{i}| \operatorname{pa}(X_{i}, G)).$ 

Model: structure and parameters (LR/MLP: $\underline{\theta}$ , BN: $\underline{\omega}$ )

Bayesian network used for parameter elicitation (conditional probabilities are underlined):





## Methods

Frequentist statistics: optimization (w.r.t. likelihood) Bayesian statistics: model averaging (w.r.t. posterior) Predictive inference:

$$p(x|D) = \sum_{k} p(M_k|D) \int p(x|\theta_k) p(\theta_k|D, M_k) \,\mathrm{d}\theta_k. \tag{1}$$

"Parametric" inference (inferring about a structural model property):

$$p(F(G) = f|D_N) = \mathbb{E}_{p(G|D_N)}[F(G) = f] = \sum_G \mathbb{1}(F(G) = f)p(G|D_N).$$
(2)

Inference	Model	Target	Method
Predictive	LR/MLP	$p(y \underline{x}, S, D_N) = E_{p(\underline{\omega} D_N)}[f(\underline{x}, \underline{\omega}]$	hybrid-MCMC
Predictive	N-BN	$p(y \underline{x}, D_N) = E_{p(G D_N)}[p(y \underline{x}, G)]$	exact (by sum-prod flip)
Predictive	BN	$p(y \underline{x}, D_N) = E_{p(G D_N)}[p(y \underline{x}, G)]$	ordering MCMC
Parametric	BN	$p(F(G) = f D_N) =$	ordering MCMC
		$E_{p(\prec D_N)}[p(F(G) = f \prec)]$	
Parametric	BN	K most probable model properties	integrated estimate&search



# **Contributions of the thesis**

#### 1. Electronic prior knowledge.

- (a) Statistical natural language processing
  - i. Text-mining by Bayesian networks (BNs).
- (b) Bayesian logic.
  - i. Fusion of factual and uncertain knowledge.

#### 2. Bayesian analysis of relevance.

- (a) Generalizations of the feature subset selection (FSS) problem.
- (b) Ordering MCMC for Markov Boundary subGraphs (MBG).
- (c) Integrated estimate and search method for MBGs and Markov Boundary sets.
- (d) The Bayesian, four-level analysis of relevance (B4s).
- 3. Fusion of prior expertise in predictive systems.
  - (a) Knowledge engineering textually enriched prior models (BNs).
  - (b) Prequential analysis of the value of priors.
  - (c) Structural priors for multilayer perceptrons (MLPs) using MBGs.
  - (d) Parametric priors for MLPs by a distance minimization projection method.



Document collections by querying Pubmed query with "ovarian cancer" (35, 562) the *most relevant* papers (2, 256) in the *most relevant* journals (2), the *highly relevant* papers (3, 301) the *highly relevant* journals (3), the *moderately relevant* papers (9, 372) in the *moderately relevant* journals (33),

the *relevant* journals papers (12, 038) in the *relevant* journals (93).

Domain vocabulary (phrases, synonyms).

Variables

Discretization levels,

"Text kernel": name, synonyms, annotations, references.

Hierarchical groupings of the variables.

Pairwise relations: relevance (existential), sign, logical/causal,

Parameterized Bayesian network: 11 variables, 400 estimates,

Three embedded BN structures: 35 variables,

Partial and complete orderings of the variables.



#### **Prior BN structures**



Dashed lines: high relevance, dashed-dotted lines: medium relevance, and dotted lines. relevance (structures are embedded).





SBDBS:SA

The scatterplot of the conditional probabilities for all the IOTA variables using the expert's estimates (vertical axis) and the posterior expectations with  $BD_{eu}$  priors (horizontal axis). The coordinates are labeled with being inside/outside (./x) a credible region(0.99).

#### The value of parameter prior: the

#### hyperposterior of the virtual sample size



Observations:

GDBS:Sy

- 1. numeric estimates worth  $\approx$  150 complete cases,
- 2. in simpler model this drops to  $\approx$ 50 cases,
- 3. even uniform pseudocounts are advantageous (corresponding to  $\approx$  10 cases).



## A multivariate, model-based, causal

#### text-mining by Bayesian networks





## Analysis of the association-cooccurrence

# relation



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# Analysis of the forward-causal assumption:

## Bayesian, sequential, pairwise approach

The temporal evolution of the collective belief — inferred from the literature — that a given variable is relevant for the preoperative diagnostics of ovarian cancer.



The figure shows the sequential posteriors of Bayesian network based relevances - the MBM(Pathology, $X_i$ ,G) relations - using the temporal sequence of publications between 1980 and 2005 in the large PubMed corpus.

#### Observations:

- 1. convergence to 0/1 corresponds well to clinical irrelevance/relevance,
- 2. high level of uncertainty >> MAP model-based evaluations are problematic!,



# Learning Bayesian network features from

#### heterogeneous sources

From prior incorporation to BN features???

- 1. Scarcity of data  $\Rightarrow$  Bayesian analysis of model properties (BN features).
- 2. 2000: Bayesian analysis of pairwise relevances  $[5, 6] \Rightarrow$  fragmentary theory.
- 3. The questions are conditional ones (relevance of "attributes" for target).
- 4. Even the prior is conditionally biased.
- 5. Idea: Bayesian analysis of restricted, but "conditionally complete" feature.





#### A probabilistic concept of relevance (the "fi lter" approach)

**Definition 1.** A feature  $X_i$  is strongly relevant, if there exists some  $x_i, y$  and  $s_i = x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n$  for which  $p(x_i, s_i) > 0$  such that  $p(y|x_i, s_i) \neq p(y|s_i)$ . A feature  $X_i$  is weakly relevant, if it is not strongly relevant, and there exists a subset of features  $S'_i$  of  $S_i$  for which there exists some  $x_i, y$  and  $s'_i$  for which  $p(x_i, s'_i) > 0$  such that  $p(y|x_i, s'_i) \neq p(y|s'_i)$ . A feature is relevant, if it is either weakly or strongly relevant; otherwise it is irrelevant [7, 8].

#### A graph-theoretic representation of relevance

BDBS:S

**Theorem 1 ([16]).** If distribution P is stable w.r.t. the DAG G, then the variables corresponding to the nodes in the boundary of Y, bd(Y, G) (the parents and children of Y and other parents of its children) forms a unique and minimal Markov blanket of Y,  $MB_P(Y)$  (the Markov boundary). Furthermore,  $X_i \in MB_P(Y)$ , if  $X_i$  is strongly relevant.

Observation (filter vs. wrapper approach): this filter approach is

- 1. model-free: independent of the function class,
- 2. method-free: independent of the optimization method,
- 3. loss-free: independent of the performance measure,



#### **Bayesian network features:**

#### pairwise, set-based, subgraph-based



<u>Multivariate with interactions (subgraph):Markov Blanket subgraph (MBG(Pathology, Multivariate (set):Markov blanket [set] (MB(Pathology,G))</u> <u>Univariate (pairwise): Markov Blanket Members MBM(Pathology,X,G)</u>

Observation: these features form a hierarchy of decreasing complexity (cardinality):  $BN \rightarrow MBG \rightarrow MBM$ 



**Proposition 1.** Under standard assumptions, the Markov Blanket structural and parametric marginals define the conditional distribution of Y given other variables  $V \setminus Y$ :  $p(Y \models V \setminus Y) \sum_{\text{MBG}(Y,G) = \text{mbg}} p(\text{mbg})p(Y \mid \text{mbg}),$ 

The space of DAGs can be collapsed to the MBG subspace in BMA ( $\mathcal{O}(n!2^{n^2}) \rightarrow$ ).

**Theorem 2 ([4]).** Under standard assumptions, the ordering-conditional posterior  $p(MBG(Y,G) = mbg \mid \prec, D_N)$  can be computed in polynomial time.

The MBG subspace can be reduced to the space of orderings in BMA ( $\rightarrow O(n!)$ ):

 $\mathbf{E}_{p(G|D_N)}[\mathrm{MBG}(Y,G) = \mathrm{mbg}] = \mathbf{E}_{p(\prec|D_N)}[p(\mathrm{MBG}(Y,G) = \mathrm{mbg} \mid \prec, D_N)]$ 

Using dynamic programming with  $\mathcal{O}(n2^n)$  space complexity [9]: The space of orderings can be reduced to space of subsets in BMA ( $\rightarrow \mathcal{O}(n2^n)$ ).



# Generalizations of the feature subset

# selection (FSS) problem I.: learn subgraph

**Definition 2.** In case of a stable distribution  $p(Y, \underline{X})$ , the feature (sub)graph selection problem (FGS) denotes the identification of a Markov Blanket subgraph MBG(Y, G), where DAG G denotes a perfect map of distribution p (i.e., Markov Blanket set + substructure).





## Generalizations of the FSS II.:

#### learn multiple, most probable features

**Definition 3.** The Most Probable Features problem (MPFs(K)) consists of the selection of K most probable feature values  $f \in \mathcal{F}$ .

The "Monte Carlo top K selection problem":

- 1. estimation of the posteriors,
- 2. optimization (search).

A statistical result using uniformly good estimates:

**Theorem 3 ([10]).** Assuming M i.i.d. samples, the expected error in MPFs(K) is

$$\mathbf{E}\left[\frac{1}{K}\left(\sum_{i=1}^{K}\hat{\mathcal{P}}_{i}-\sum_{i=1}^{K}\mathcal{P}_{i}^{*}\right)\right] \leq \sqrt{\frac{\log(2|\mathcal{F}|)+1}{M/2}}$$

An algorithm for MPFs-MBG(K):

Integrated estimation and search using the MBG-ordering spaces [3].



# A method for the integrated estimation and

# search for MBGs (MBs)

**Require:**  $p(\prec), p(pa(X_i) | \prec), k, R, \rho, L^S, \rho^S, L^T, M;$ **Ensure:** K MAP feature value with estimates for l = 0 to M do {the sampling cycle} Draw next ordering; Compute  $p(\prec_l | D_N)$ ; Construct order conditional MBG-Subspace  $(\Pi, \Psi, R, \rho) = \Phi$  $S^{S}$ =UniformCostSearch( $\Phi$ , $L^{S}$ , $\rho^{S}$ ); for all  $mbg \in S^S$  do if  $mbg \notin \mathcal{T}$  then lnsert(T, mbg)if  $L^T < |\mathcal{T}|$  then  $\mathcal{T}$ =PruneToHPD( $\mathcal{T}, L^T$ ); for all  $mbg \in \mathcal{T}$  do  $\hat{p}(mbg|D_N) + = p(mbg| \prec_l, D_N);$ 



# Why Bayesian? Uncertainty at all levels.

The relative log posteriors of ranked BNs, MBs, MBGs.



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- 1. numeric approximation is tragic,
- 2. approximation of rankings is poor,
- 3. particularly in the unconstrained case,
- 4. In general: MAP-MBG≠MBG(MAP-BN), MAP-MB≠MB(MAP-MBG)≠MB(MAP-BN), MAP-MBM≠MBM(MAP-MB)≠...



# The sequential analysis of relevance:

# the pairwise (MBM) level

The temporal evolution of the belief — represented by the posterior of the MBM feature and inferred from growing amount of clinical data — that a given variable is relevant for the preoperative diagnostics of ovarian cancer (conditional on the expert's ordering).



The horizontal axis is the sample size with step size 10. *Observations:* 

- 1. non-monotonic behaviour (Age replacing Meno),
- 2. uncertainty even for all data,
- 3. trends after 500 cases,
- 4. corresponds well to expert's rating of relevance.

![](_page_26_Picture_0.jpeg)

## The sequential analysis of relevance:

the set (MB) level

The sequential posteriors of high-scoring MB(Pathology) feature values using the temporal sequence of the IOTA-1.2 data set and given the expert's total causal ordering.

![](_page_26_Figure_4.jpeg)

- 1. The posteriors are less than  $10^{-6}$  for sample size less than 400,
- 2. uncertainty even for all data, BUT POSTERIORS can be used to support the optimized design of subsequent studies.

![](_page_27_Picture_0.jpeg)

# Informative priors for parametric black-box

# models

Goals:

- 1. improved Bayesian prediction,
- 2. fair Bayesian model comparison,
- 3. model interpretation,
- 4. bridging the gap between symbolic and sub-symbolic knowledge representation.

(Some) related works:

- 1. Knowledge-Based Artificial Neural Network [15],
- 2. Bayesian networks with neural local models [14],
- 3. Mapping of Bayesian networks onto stochastic neural networks [11],
- 4. Mixture of Experts [17],
- 5. Incorporating Prior Information by Creating Virtual Examples [13],
- 6. Donor-receiver link by imaginary samples [12].

![](_page_28_Picture_0.jpeg)

## The two-step, Bayesian methodology for the

# fusion of knowledge and data

![](_page_28_Figure_3.jpeg)

First, we formalized the prior domain knowledge in a Bayesian network. Second, we induced informative structure and parameter priors for parametric conditional models to support various Bayesian inferences.

![](_page_29_Picture_0.jpeg)

#### The prior sample/sample prior

#### transformations

**Definition 4.** 

$$P(\omega|D_{N'}^+, D_N, \xi^-) \propto P(D_N|\omega) P(\omega|D_{N'}^+, \xi^-) = P(D_N|\omega, \xi^-) P'(\omega|\xi^-).$$
(4)

**Definition 5.** 

$$p(\omega|\xi^{+}) \triangleq \sum_{D_{N'}^{+}} p(\omega|D_{N'}^{+},\xi^{-}) p(D_{N'}^{+}|\xi^{+})$$
(5)

$$= \sum_{D_{N'}^+} p(\omega|D_{N'}^+, \xi^-) \int p(D_{N'}^+|\theta) p(\theta|\xi^+) \,\mathrm{d}\theta \tag{6}$$

$$\propto \sum_{D_{N'}^+} p(\omega|\xi^-) p(D_{N'}^+|\omega) \int p(D_{N'}^+|\theta) p(\theta|\xi^+) \,\mathrm{d}\theta.$$
(7)

![](_page_30_Picture_0.jpeg)

# The conditional distance minimization

#### transformation

**Definition 6 ([1, 2]).** Let  $\theta$  and  $\omega$  denote the parameters of a domain model and a conditional model. The direct transformation of an informative prior from a domain model into an informative prior over a parametric black box conditional model ( $\mathcal{T} : \Theta \to \Omega$ ) is defined as

$$\mathcal{I}_{\mathrm{KL}}(\theta) = \arg\min_{\omega'} \mathrm{E}_{p(X|\theta)} [\mathrm{KL}(p(Y|X,\omega') \| p(Y|X,\theta))] + c(\omega)$$
(8)

$$\mathcal{T}_{L_2}(\theta) = \arg\min_{\omega'} \mathbb{E}_{p(X|\theta)} [L_2(p(Y|X,\omega'), p(Y|X,\theta))] + c(\omega).$$
(9)

1, Generate Bayesian network parameters  $\{\theta_1, \ldots, \theta_l\}$ 

2, Generate block of prior samples from each parameter  $\{D_1^p, \ldots, D_l^p\}$ 

3, Train a multilayer preceptron for each block of samples resulting in a block of perceptron parameters  $\{\omega_1, \ldots, \omega_l\}$ 

3, Approximate the posterior with mixture of Gaussians (G.Fannes:symmetries in the MLP parameter space).

![](_page_31_Picture_0.jpeg)

# Performance of Bayesian classification with

# informative priors

The learning curves for the multilayer perceptron models using an informative prior (MLP-Informative), a noninformative prior (MLP-Noninformative) or prior samples (MLP-Prior sample).

![](_page_31_Figure_4.jpeg)

- 1. the same performance as the prior Bayesian network,
- 2. better performance throughout,
- 3. not restrictive in the large sample region,
- 4. high computational complexity of deriving the informative prior,
- 5. lower complexity in the inference,
- 6. collapse of a complex general Bayesian model into a task specific, simpler conditional model. INTEGRATIVE ANALYSIS OF DATA, LITERATURE, AND EXPERT KNOWLEDGE BY BAYESIAN NETWORKS p. 32/41

![](_page_32_Picture_0.jpeg)

- 1.  $10^5$  lines of code written in C++ and MATLAB,
- 2. graphical user interface in the MS-Windows MFC environment,
- 3. command line version runs in a parallel computing grid environment,
- 4. Software Environment for Bayesian and Neural Networks (SEBANN),
- 5. LINUX version with continuous variables (Geert Fannes),
- 6. System for Probabilistic Annotated Networks (SPAN),
- 7. modules are migrated into the GEnomic Study Design and Analysis platform.

![](_page_33_Picture_0.jpeg)

#### 1. Statistical text-mining of multivariate relations.

- (a) Text-mining by Bayesian networks.
- (b) Goals: minimal preparation, early applicability, model-based.

#### 2. Bayesian four-level analysis of relevance.

- (a) Integrated estimate and search method for MBGs and Markov Boundary sets.
- (b) Goals: expression, representation, and communication (publishing) of uncertainty at multiple, linked levels.

#### 3. Fusion of **electronic**, factual knowledge and probabilistic data analysis.

- (a) Bayesian logic by annotated Bayesian networks.
- (b) Goal: knowledge-rich data analysis using complex, semantical hypotheses.
- 4. Fusion of prior expertise in predictive systems.
  - (a) Fusion using the conditional distance minimization transformation.
  - (b) Goal:Fusing clinical diagnostic knowledge into models developed by high-throughput data.

![](_page_34_Picture_0.jpeg)

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- 1. Text-mining by Bayesian networks.
  - (a) Neutral omission,
  - (b) Negation,
  - (c) Temporality,
  - (d) Utility models,
- 2. Bayesian analysis of relevance.
  - (a) Multiple target variables,
  - (b) Continuous variables,
  - (c) Incomplete data,
  - (d) Scaling up the number of variables from 100 to 1000: hierarchical-MCMC and coupled-MCMC.

![](_page_35_Picture_0.jpeg)

# Acknowledgment

Thank you for your attention!

Thank you for your support.

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![](_page_36_Picture_0.jpeg)

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![](_page_37_Picture_0.jpeg)

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![](_page_38_Picture_0.jpeg)

## of relevance

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![](_page_39_Picture_0.jpeg)

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![](_page_40_Picture_0.jpeg)

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